1. Previous Midterm (by Prof. Simon). The circuit below has an AC voltage source, where $V=V_{0} \cos (\omega t)$.

(a) What is the circuit's total impedance, magnitude and phase angle? [8 points]
(b) Give an expression for the current $I(t)$ in the circuit. [8]
(c) What is the average power deliverd by the voltage source? [4]
(d) If there is a resonant frequency, what is it? [7]
2. Previous Midterm (by Prof. Simon). An electric field in air $E_{p}$, polarized at 45 degrees in the $\mathrm{x}-\mathrm{y}$ plane and moving in the -z direction can be written as

$$
\begin{equation*}
\vec{E}(z, t)=(\hat{x}+\hat{y}) E_{0} \cos (k z+\omega t) \tag{1}
\end{equation*}
$$

Here, $E_{0}=E_{p} \cos \left(\frac{\pi}{4}\right)=E_{p} \sin \left(\frac{\pi}{4}\right)$. The linearly polarized light is incident on a birefringent crystal, which has has two different indexes of refraction, $n_{x}$ for the electric field aligned with the x -axis and $n_{y}$ for the electric field along the y -axis. (a) Find the crystal thickness z which will cause a $2 \pi / 4$ (or quarter wave) phase difference for the two polarizations of light with a free space wavelength of $\lambda_{0}$. [10]

(b) Assume the crystal thickness is a quarter wave plate for a free-space $\lambda_{0}$, shifting the x - and y-components by 90 degrees. Write an expression for the electric field after the light exits the crystal. Assume that $n_{x}>n_{y}$ in the crystal. [10]
(c) A $40 \mu m$ layer of cellophane tape acts as a half wave plate ( $\pi$ phase difference) for red light passing through it. Show graphically by vector addition that the initial 45 degree linear polarization of the entering wave is rotated by 90 degrees by a half wave plate. [6]

